Today you and your partner will be running empirical experiments to determine the best, worst, and average time complexity for three different algorithms: linear search, binary search, and a median finding algorithm. Recall that for a searching or sorting algorithm, the *time complexity* is the number of comparisons made as a function of the input array size. In class, we computed the best-case and worst-case time complexity for Linear Search and Binary Search:

<table>
<thead>
<tr>
<th>Algorithm</th>
<th>Best</th>
<th>Worst</th>
<th>Average</th>
</tr>
</thead>
<tbody>
<tr>
<td>Linear Search</td>
<td>1</td>
<td>$n$</td>
<td>$\frac{n}{2}$</td>
</tr>
<tr>
<td>Binary Search</td>
<td>1</td>
<td>$\log_2(n)$</td>
<td>?</td>
</tr>
</tbody>
</table>

where $n$ is the size of the array.

In this lab, you will actually count the number of comparisons as the array size varies and then generate plots (and write a “lab report”) documenting what you found. At the end of this lab, please submit whatever you and your partner were able to accomplish.

### 1 Step 0: Familiarizing Yourself

*Do not begin the steps below until you have read through each of the methods in the two Java classes provided!*

- Read through the methods in the `ListSearcher` class.
- Read through the methods in the `PerformanceTester` class.

Make sure you understand what each class is doing, what the methods do, and what the instance variables represent. If you have any questions, call me or the lab assistant over.

### 2 Step 1: Counting Comparisons

You will notice that there is no code for actually counting the number of comparisons in the `ListSearcher` class. This is your first task.

1. Add an instance variable to the `ListSearch` class to keep track of the number of comparisons made.

2. Modify the `linearSearch()`, `binarySearch()`, and `findMedian()` methods so that they count how many comparisons are made. Conceptually, a “comparison” is any time we access an element in the array and compare its value to something else.

   Thus, for Binary Search you have a choice. You can count each iteration of the while loop as 2 comparisons – since in the code itself we access `array[mid]` twice and each time compare its value – or you can count each iteration of the while loop as 1 comparison – since conceptually each iteration of the while loop compares $k$ to `array[mid]`. The latter option (each iteration = 1 comparison) is the more standard way of counting comparisons.

3. Finally, add the following accessor/mutator methods:
• public int getComparisons() - This method returns the number of comparisons made
• public void resetComparisons() - This method resets the number of comparisons to 0.

You are now able to reset, count, and get the number of comparisons made.

3 Step 2: Running Experiments

Now that you can count comparisons, let’s test to see if our analysis of the time complexity of linear and binary search are actually correct.

The PerformanceTester class has three static methods: testLinearSearch, testBinarySearch, and testMedian. This section will step you through experimenting with linear search. Once you learn how to do this, you can go back and do the same for binary search. (Ignore the median method for now.)

Look inside the main method. You’ll see that we’re calling testLinearSearch with an array of size N=1000, number of trials equal to 1, and unordered data. If you run the main method, you should see something similar to the following print out:

N=1000, best=333 (expected 1), worst=333 (expected 1000), avg=333 (expected 500)

Let’s actually spend a little bit of time understanding the report we just generated above. Recall our hypothesis that the best case, worst case, and average case comparisons for linear search are 1, n, and n/2, respectively.

In the report printed out, the best, worst, and average number of comparisons are all the same because linearSearch() was only run once. As a result, the quality of these results is not very good, and as computer scientists, we know that results from a single experiment cannot be taken at face value! A good scientist would repeat the experiment multiple times to get a good understanding of what’s really happening.

• Modify the input values to testLinearSearch to repeat the experiment 10 times. The report printed out should show values closer to the expected number of comparisons.

• Open up the Word document included in the starter code and answer question Q1.

Generating Plots

It would be great to generate plots to better visualize our results. Open up your favorite spreadsheet tool, like Sheets on Google Docs or Excel. The following example shows how to generate charts using Sheets on Google Docs:

• In main, call testLinearSearch for N = 1000, 2000, 3000, . . . , 10000 using the number of trials you found worked best in question Q1.

• Head over to Google Docs. One of you will need a Google ID to sign in. Once in, click on the striped-lines button on the top-left corner, and select Sheets. Next, click on the + button and it should generate a new blank spreadsheet. Let us know if you have troubles getting this far.

• After you’ve got a blank sheet in front of you, copy the numbers for N, best case, worst case, and average case as follows:
• Double-check that all of your data is entered correctly. Then highlight your data (including the first row containing labels). From the menu bar, click “Insert > Chart”. Click on the “Chart Types” tab at the top and select the first “Line” box to generate a line plot. Scroll down and make sure that “Use row 1 as headers” and “Use column A as labels” are both checked.

• Click on the “Customise” tab at the top. Click on the “Chart & axis titles” dropdown menu to give your chart a title. Label the horizontal axis “N (List Size)” and your vertical axis “Comparisons”. That’s it, you now have a chart! See below for an image of what your chart should look like.
• Click on the chart, and in the top-right hand corner you should see three vertical dots. Click on this icon, and select “Download as” and download the chart as a PNG file. Open the downloaded file and drag the chart into the appropriate place in your lab report under Q2.

• That’s all there is! Go ahead and answer Q3 in your lab report. This question asks you to experiment with linear search using ordered (i.e. sorted) data.
4 Step 3: Binary Search

Alright, now do this all over again but this time with binary search.

Notice that testBinarySearch has no boolean flag to indicate whether it should generate ordered or unordered data because binary search requires an ordered array to work correctly. Run this method for \( N = 1000, 2000, 3000, \ldots, 10000 \). Generate a plot and add it to your report. Answer question \( Q4 \).

5 Analyzing a New Algorithm

This last section asks you to analyze a brand new algorithm: an algorithm to find the median value in an array. The median of a set of numbers is the number that is bigger than half the values and smaller than half the values. If the array was sorted, the median would be in the middle spot. Note: If the array has even length, there is no unique median. In this case, either of the middle values would work.

1. Open up the ListSearcher class and read the findMedian() code. This is a very naive algorithm for finding the median!
2. Make a guess for the best, worst, and average time complexity for this method. Record your guess in your lab report.
3. Run experiments by calling the testMedian method in the PerformanceTester class using \( N = 100, 200, 300, \ldots, 1000 \). If you run bigger values, it will take a long time to complete. Try to run as many trials as possible.
4. Open your spreadsheet program, and generate another plot, with the best, worst, and average-case. Insert the plot in your Lab Report, and answer the final question.

6 Submitting your lab assignment

Submit your lab11 folder with both Java classes and your Word lab report inside. Remember to put both of your names on the folder before you zip it. Submit via Canvas.